

**Def.** The first uncertain digit are known as **significant digits** or **significant figures**. If we say the period of oscillation of a simple pendulum is 1.62 s, the digits 1 and 6 are reliable and certain, while the digit 2 is uncertain. Thus, the measured value has three significant figures. The length of an object reported after measurement to be 287.5 cm has four significant figures, the digits 2, 8, 7 are certain while the digit 5 is uncertain. **Clearly, reporting the result of measurement that includes more digits than the significant digits is superfluous and also misleading since it would give a wrong idea about the precision of measurement.**

**The rules for determining the number of significant figures** can be understood from the following examples. **Significant figures indicate, as already mentioned, the precision of measurement which depends on the least count of the measuring instrument. A choice of change of different units does not change the number of significant digits or figures in a measurement.** This important remark makes most of the following observations clear:

(1) For example, the length 2.308 cm has four significant figures. But in different units, the same value can be written as 0.02308 m or 23.08 mm or 23080  $\mu\text{m}$ .

All these numbers have the same number of significant figures (digits 2, 3, 0, 8), namely four. This shows that the location of decimal point is of no consequence in determining the number of significant figures.

The example gives the following **rules** :

- **All the non-zero digits are significant.**
- **All the zeros between two non-zero digits are significant, no matter where the decimal point is, if at all.**
- **If the number is less than 1, the zero(s) on the right of decimal point but to the left of the first non-zero digit are not significant.** [In 0.00 2308, the underlined zeroes are not significant].
- **The terminal or trailing zero(s) in a number without a decimal point are not significant.**

[Thus 123 m = 12300 cm = 123000 mm has three significant figures, the trailing zero(s) being not significant.] However, you can also see the next observation.

- **The trailing zero(s) in a number with a decimal point are significant.**

[The numbers 3.500 or 0.06900 have four significant figures each.]

(2) There can be some confusion regarding the trailing zero(s). Suppose a length is reported to be 4.700 m. It is evident that the zeroes here are meant to convey the precision of measurement and are, therefore, significant. [If these were not, it would be superfluous to write them explicitly, the reported measurement would have been simply 4.7 m]. Now suppose we change units, then

$$4.700 \text{ m} = 470.0 \text{ cm} = 4700 \text{ mm} = 0.004700 \text{ km}$$

Since the last number has trailing zero(s) in a number with no decimal, we would conclude erroneously from observation (1) above that the number has *two* significant figures, while in fact, it has four significant figures and a mere change of units cannot change the number of significant figures.

(3) **To remove such ambiguities in determining the number of significant figures, the best way is to report every measurement in scientific notation (in the power of 10).** In this notation, every number is expressed as  $a \times 10^b$ , where  $a$  is a number between 1 and 10, and  $b$  is any positive or negative exponent (or power) of 10. In order to get an approximate idea of the number, we may round off the number  $a$  to 1 (for  $a \leq 5$ ) and to 10 (for  $5 < a \leq 10$ ). Then the number can be expressed approximately as  $10^b$  in which the exponent (or power)  $b$  of 10 is called **order of magnitude** of the physical quantity. When only an estimate is required, the quantity is of the order of  $10^b$ . For example, the diameter of the earth ( $1.28 \times 10^7 \text{ m}$ ) is of the order of  $10^7 \text{ m}$  with the order of magnitude 7. The diameter of hydrogen atom ( $1.06 \times 10^{-10} \text{ m}$ ) is of the order of  $10^{-10} \text{ m}$ , with the order of magnitude -10. Thus, the diameter of the earth is 17 orders of magnitude larger than the hydrogen atom.

It is often customary to write the decimal after the first digit. Now the confusion mentioned in (a) above disappears :

$$\begin{aligned} 4.700 \text{ m} &= 4.700 \times 10^2 \text{ cm} \\ &= 4.700 \times 10^3 \text{ mm} = 4.700 \times 10^{-3} \text{ km} \end{aligned}$$

The power of 10 is irrelevant to the determination of significant figures. However, all