

$$v = u + at; \quad s = ut + \frac{1}{2}at^2 \quad \text{and} \quad v^2 = u^2 + 2as$$

$$\text{reduces to } 0 = u - gt \quad h = ut - \frac{1}{2}gt^2 \quad \text{and} \quad 0 = u^2 - 2gh$$

[the velocity at the highest point is  $v = 0$ ]

From the above equations we get

$$u = gt \quad \dots \quad (4)$$

$$h = \frac{1}{2}gt^2 \quad \dots \quad (5)$$

$$u^2 = 2gh \quad \dots \quad (6)$$

These equations can be used to solve most of the problems of bodies projected vertically up. Let us summarise the above as: If the initial velocity of projection is given, we get three simple equations as:

$$h = \frac{u^2}{2g} \dots\dots\dots[7] \quad , \quad t = \frac{u}{g} \dots\dots\dots[8] \quad \text{or} \quad t = \sqrt{\frac{2h}{g}} \dots\dots\dots[9]$$

### **IMPORTANT POINTS**

- (1) In case of motion under gravity for a given body, mass, acceleration, and mechanical energy remain constant while speed, velocity, momentum, kinetic energy and potential energy change.
- (2) The motion is independent of the mass of the body, as in any equation of motion, mass is not involved. This is why a heavy and lighter body when released from the same height, reach the ground simultaneously and with same velocity.

i.e  $t = \sqrt{(2h/g)}$  and  $v = \sqrt{2gh}$

**However, momentum, kinetic energy or potential energy depend on the mass of the body ( all  $\propto$  mass)**

- (3) As from equation (5) time taken to reach a height  $h$ ,

$$t_u = \sqrt{(2h/g)}$$

Similarly, time taken to fall down through a distance  $h$  [from Eq(2)],