## Dual Nature of Radiation and Matter

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$$eV_0 = hv - \phi_0 = \frac{hc}{\lambda} - \phi_0$$
  
or,  $\lambda = hc/(eV_0 + \phi_0)$   
$$= \frac{(6.63 \times 10^{-34} \text{ J s}) \times (3 \times 10^8 \text{ m/s})}{(0.60 \text{ eV} + 2.14 \text{ eV})}$$
  
$$= \frac{19.89 \times 10^{-26} \text{ J m}}{(2.74 \text{ eV})}$$
  
 $\lambda = \frac{19.89 \times 10^{-26} \text{ J m}}{2.74 \times 1.6 \times 10^{-19} \text{ J}} = 454 \text{ nm}$ 

**Example 11.3** The wavelength of light in the visible region is about 390 nm for violet colour, about 550 nm (average wavelength) for yellowgreen colour and about 760 nm for red colour.

- (a) What are the energies of photons in (eV) at the (i) violet end, (ii) average wavelength, yellow-green colour, and (iii) red end of the visible spectrum? (Take  $h = 6.63 \times 10^{-34}$  J s and 1 eV =  $1.6 \times 10^{-19}$  J.)
- (b) From which of the photosensitive materials with work functions listed in Table 11.1 and using the results of (i), (ii) and (iii) of (a), can you build a photoelectric device that operates with visible light?

## Solution

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(ii) For

(a) Energy of the incident photon,  $E = hv = hc/\lambda$  $E = (6.63 \times 10^{-34} \text{J s}) (3 \times 10^8 \text{ m/s})/\lambda$ 

$$\frac{1.989 \times 10^{-25} \text{ Jm}}{\lambda}$$

(i) For violet light,  $\lambda_1 = 390$  nm (lower wavelength end)

ident photon energy, 
$$E_1 = \frac{1.989 \times 10^{-25} \text{ J m}}{390 \times 10^{-9} \text{ m}}$$
  
= 5.10 × 10<sup>-19</sup> J  
=  $\frac{5.10 \times 10^{-19} \text{ J}}{1.6 \times 10^{-19} \text{ J/eV}}$   
= 3.19 eV  
yellow-green light,  $\lambda_2$  = 550 nm (average wavelength)

Incident photon energy,  $E_2 = \frac{1.989 \times 10^{-25} \text{ Jm}}{550 \times 10^{-9} \text{ m}}$ = 3.62×10<sup>-19</sup> J = 2.26 eV

(iii) For red light,  $\lambda_3 = 760$  nm (higher wavelength end)

Encident photon energy, 
$$E_3 = \frac{1.989 \times 10^{-25} \text{ Jm}}{760 \times 10^{-9} \text{ m}}$$
  
= 2.62×10<sup>-19</sup> J = 1.64 eV

(b) For a photoelectric device to operate, we require incident light energy *E* to be equal to or greater than the work function  $\phi_0$  of the material. Thus, the photoelectric device will operate with violet light (with E = 3.19 eV) photosensitive material Na (with  $\phi_0 = 2.75 \text{ eV}$ ), K (with  $\phi_0 = 2.30 \text{ eV}$ ) and Cs (with  $\phi_0 = 2.14 \text{ eV}$ ). It will also operate with yellow-green light (with E = 2.26 eV) for Cs (with  $\phi_0 = 2.14 \text{ eV}$ ) only. However, it will not operate with red light (with E = 1.64 eV) for any of these photosensitive materials.