

Fig. 14.4 The location of the particle in SHM at the discrete values $t = 0, T/4, T/2, 3T/4, T, 5T/4$. The time after which motion repeats itself is T . T will remain fixed, no matter what location you choose as the initial ($t = 0$) location. The speed is maximum for zero displacement (at $x = 0$) and zero at the extremes of motion.

of motion. Fig. 14.5 plots the graph of x versus t , which gives the values of displacement as a continuous function of time. The quantities A , ω and ϕ which characterize a given SHM have standard names, as summarised in Fig. 14.6. Let us understand these quantities.

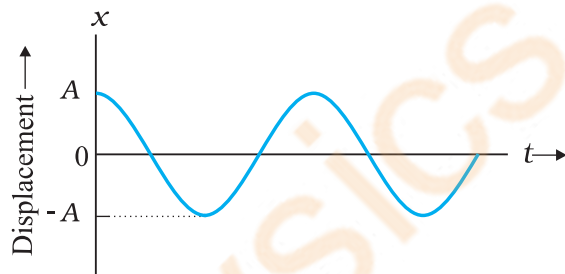


Fig. 14.5 Displacement as a continuous function of time for simple harmonic motion.

$x(t)$: displacement x as a function of time t
A	: amplitude
ω	: angular frequency
$\omega t + \phi$: phase (time-dependent)
ϕ	: phase constant

Fig. 14.6 The meaning of standard symbols in Eq. (14.4)

The amplitude A of SHM is the magnitude of maximum displacement of the particle. [Note, A can be taken to be positive without any loss of generality]. As the cosine function of time varies from $+1$ to -1 , the displacement varies between the extremes A and $-A$. Two simple harmonic motions may have same ω and ϕ but different amplitudes A and B , as shown in Fig. 14.7 (a).

Amplitude

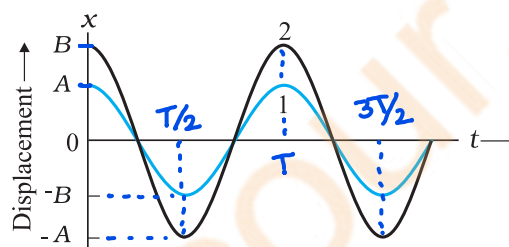


Fig. 14.7 (a) A plot of displacement as a function of time as obtained from Eq. (14.4) with $\phi = 0$. The curves 1 and 2 are for two different amplitudes A and B .

While the amplitude A is fixed for a given SHM, the state of motion (position and velocity) of the particle at any time t is determined by the argument $(\omega t + \phi)$ in the cosine function. This time-dependent quantity, $(\omega t + \phi)$ is called the phase of the motion. The value of phase at $t = 0$ is ϕ and is called the phase constant (or phase angle). If the amplitude is known, ϕ can be determined from the displacement at $t = 0$. Two simple harmonic motions may have the same A and ω but different phase angle ϕ , as shown in Fig. 14.7 (b).

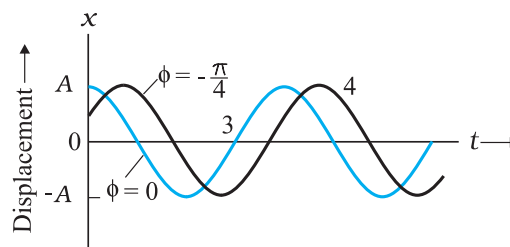


Fig. 14.7 (b) A plot obtained from Eq. (14.4). The curves 3 and 4 are for $\phi = 0$ and $-\pi/4$ respectively. The amplitude A is same for both the plots.