

Solution: In this case force is variable (function of x). So, let's use eq.(4)

$$W = \int_2^4 (3x + 4).dx = \left[\frac{3x^2}{2} \right]_2^4 + [4x]_2^4$$

$$W = \left(\frac{3 \times 4^2}{2} - \frac{3 \times 2^2}{2} \right) + [4(4 - 2)] = 26J$$

Example 3: A man weighing 70 kg carries a 30 kg box to the top of a building 20 m high. Calculate the work done by the man. Take $g = 9.8 \text{ ms}^{-2}$. **Ans:** 19600 J.

Solution: The total upward force applied by the man = weight of the man + weight of the box

$$\begin{aligned} \text{So, the net upward force (F)} &= Mg + mg = 70 \times 9.8 + 30 \times 9.8 \\ &= 980 \text{ N} \end{aligned}$$

Net upward displacement (S) = 20m

Since, force and the displacement are in the same direction, $\theta = 0^\circ$.

Since,
$$W = F.S \cos \theta$$

$$W = 980 \times 20 \times \cos 0^\circ = 19600J$$

Example 4: A body constrained to move along the z-axis of a coordinate system is subject to a constant force F given by

$$\mathbf{F} = -\hat{i} + 2\hat{j} + 3\hat{k} \text{ N}$$

Where, \hat{i}, \hat{j} and \hat{k} are unit vectors along the x-, y- and z-axis of the system respectively. What is the work done by this force in moving the body a distance of 4 m along the z-axis?

(NCERT) Ans. 12 J

Solution: Since the body is constrained to move along the z-axis, the displacement vector is $\vec{S} = 4\hat{k}$. So work done is