

$$[x]_{x_0}^x = \int_0^t v_0 \cdot dt + \int_0^t at \cdot dt$$

OR

$$x - x_0 = v_0 [t]_0^t + a \left[\frac{t^2}{2} \right]_0^t$$

OR

$$x - x_0 = v_0 (t - 0) + a \left(\frac{t^2}{2} - 0 \right)$$

$$\mathbf{x - x_0 = v_0 t + (1/2) at^2}$$

$$\text{(iii) } \mathbf{V^2 = u^2 + 2aS} \quad \text{or} \quad \mathbf{V^2 = v_0^2 + 2a(x - x_0)}$$

By definition

$$a = \frac{dv}{dt} \quad \text{Or} \quad a = \frac{dv}{dx} \cdot \frac{dx}{dt}$$

$$\text{Or} \quad a = v \cdot \frac{dv}{dx} \quad \text{Or} \quad v \cdot dv = a \cdot dx$$

Integrating both sides

$$\int_{V_0}^V v \cdot dv = \int_{x_0}^x a \cdot dx$$

$$\left[\frac{v^2}{2} \right]_{V_0}^V = a \int_{x_0}^x dx \quad \text{OR} \quad \frac{v^2}{2} - \frac{v_0^2}{2} = a [x]_{x_0}^x$$

$$\frac{1}{2}(v^2 - v_0^2) = a(x - x_0)$$

$$\text{Or} \quad v^2 - v_0^2 = 2a(x - x_0)$$

$$\text{Or} \quad v^2 = v_0^2 + 2a(x - x_0)$$