So, the condition for nth bright fringe becomes $\Delta x_{optical} = \pm n\lambda$

$$\left(\frac{d \cdot y_n}{D}\right) - (\mu - 1)t = \pm n\lambda$$

$$\Rightarrow \quad y_n = \pm n\frac{\lambda D}{d} + \frac{D(\mu - 1)t}{d}$$

$$\Rightarrow n^{\text{th}} \text{ fringe is shifted by } \Delta y_0 = \frac{D(\mu - 1)t}{d}$$

As
$$\beta = \frac{D\lambda}{d}$$
, also $\Delta y_0 = \frac{\beta}{\lambda} (\mu - 1) t$

Note: Thus by the introduction of a thin glass plate in front of any slit, the fringe width does not change. However, the whole pattern shifts by a distance of $\frac{(\mu - 1)tD}{d}$

The shift of the pattern is towards that side where the thin transparent plate is introduced. More the refractive index of the material of plate more is the shift.