

$$(dv)^{\gamma-1} \Rightarrow \left(\frac{dv}{dV}\right) \cdot V = -1$$

$$\frac{dP}{dV} = -\frac{P}{V} \quad \text{--- (3)}$$

Slope of Isothermal curve $(\text{slope})_{iso} = -\frac{P}{V} \quad \text{--- (4)}$

For adiabatic Process : $PV^{\gamma} = K' \quad \text{--- (5)}$

$$P \cdot \frac{dV^{\gamma}}{dV} + \left(\frac{dP}{dV}\right) \cdot V^{\gamma} = 0 \quad \left\{ \begin{array}{l} \frac{d x^n}{d x} = n x^{n-1} \end{array} \right.$$

$$P \{ \gamma \cdot V^{\gamma-1} \} + \frac{dP}{dV} \cdot V^{\gamma} = 0$$

$$\frac{dP}{dV} \cdot V^{\gamma} = -P \gamma \cdot V^{\gamma-1}$$

$$\frac{dP}{dV} = -P \cdot \gamma \cdot \frac{V^{\gamma-1}}{V^{\gamma}}$$

$$\frac{dP}{dV} = -\gamma \frac{P}{V} \quad \text{--- (6)}$$

$$(\text{slope})_{adia} = -\gamma \frac{P}{V} \quad \text{--- (7)}$$

hence $(\text{slope})_{adia} / (\text{slope})_{iso} = -\gamma \left(\frac{P}{V}\right) / \left(-\frac{P}{V}\right)$