

$$\text{or } \rho = \rho_0 (1 - \gamma \cdot \Delta T) \quad \text{--- (13)}$$

Example: The coefficient of volume expansion of glycerin is $49 \times 10^{-5} \text{ K}^{-1}$. What is the fractional change in its density for a 30°C rise in temperature? [NCERT Exercise]

Given

$$\gamma = 49 \times 10^{-5} \text{ K}^{-1}$$

$$\Delta T = 30^\circ \text{C}$$

$$\therefore \rho = \rho_0 (1 - \gamma \cdot \Delta T)$$

$$\rho = \rho_0 - \rho_0 \gamma \Delta T$$

$$\Delta \rho = \rho - \rho_0 = -\rho_0 \cdot \gamma \cdot \Delta T$$

$$\begin{aligned} \text{Fractional change in density} &= \frac{\text{change in density}}{\text{original density}} \\ &= \frac{\Delta \rho}{\rho_0} = ? \end{aligned}$$

$$\text{Fractional change} = \frac{\Delta \rho}{\rho_0} = \frac{-\cancel{\rho_0} \gamma \Delta T}{\cancel{\rho_0}} = -\gamma \cdot \Delta T$$

$$= -49 \times 10^{-5} \times 30 = -1470 \times 10^{-5}$$

$$= -1.47 \times 10^{-2}$$

Anomalous Expansion of water: 4°C to 0°C

