

Example: Moment of inertia of a ring is $3 \text{ kg}\cdot\text{m}^2$.

It is rotated for 20 sec by a torque of $6 \text{ N}\cdot\text{m}$.

Calculate the work done. [Ans: 2400 J]

$$I = 3 \text{ kg}\cdot\text{m}^2, t = 20 \text{ sec}$$

$$\tau = 6 \text{ N}\cdot\text{m}$$

$$\begin{array}{l} m \rightarrow I \\ v \rightarrow \omega \\ a \rightarrow \alpha \\ p \rightarrow L \\ F \rightarrow \tau \end{array}$$

$$\begin{array}{l} x \rightarrow \theta \\ \Delta x \rightarrow \Delta \theta \end{array}$$

$$\Delta W = F \cdot \Delta x \rightarrow \boxed{\Delta W_{\text{rot}} = \tau \cdot \Delta \theta}$$

$$dW_{\text{rot}} = \tau \cdot d\theta$$

$$W = \int_{x_1}^{x_2} F \cdot dx \rightarrow \boxed{W_{\text{rot}} = \int_{\theta_1}^{\theta_2} \tau \cdot d\theta}$$

Work Energy Theorem

$$W_{\text{total}} = K_f - K_i \rightarrow W_{\text{rot}} = K_{f\text{rot}} - K_{i\text{rot}}$$

$$K = \frac{1}{2} I \omega^2$$

$$W = K_f - K_i$$

$$\boxed{W_{\text{rot}} = \frac{1}{2} I_f \omega_f^2 - \frac{1}{2} I_i \omega_i^2}$$

Given:

$$\omega_i = 0, \omega_f = ?, I = 3 \text{ kg}\cdot\text{m}^2$$

$$\tau = 6 \text{ N}\cdot\text{m}, t = 20 \text{ sec}, W_{\text{rot}} = ?$$

$$\because \tau = I\alpha \Rightarrow \alpha = \frac{\tau}{I} \Rightarrow \alpha = \frac{6}{3} \Rightarrow \alpha = 2 \text{ rad/s}^2$$