

velocity at the end of five seconds.

[Ans: 4 rev/s², 20 rev/s]

$$\Delta\theta = 50 \text{ rev}$$

$$\Delta\theta = 50 \times 2\pi \text{ rad}$$

$$\Delta\theta = 100\pi \text{ rad}$$

$$\alpha = ? , \omega = ?$$

$$\Delta\theta = \omega_0 t + \frac{1}{2} \alpha t^2$$

$$100\pi = 0 + \frac{1}{2} \cdot \alpha \cdot (5)^2$$

$$200\pi = 25\alpha \Rightarrow \alpha = \frac{200\pi}{25} = 8\pi \text{ rad/s}^2$$

$$\alpha = \frac{8\pi}{2\pi} \text{ rev/s}^2 \Rightarrow \alpha = 4 \text{ rev/s}^2$$

$$\omega = \omega_0 + \alpha t \Rightarrow \omega = 0 + 8\pi \times 5 \Rightarrow \omega = 0 + 40\pi$$

$$\omega = \frac{40\pi}{2\pi} = 20 \text{ rev/s}$$

$$\omega = 40\pi \text{ rad/s}$$

Ex2

A body rotates about a fixed axis with an angular acceleration of one radian/second². Through what angle does it rotate during the time in which its angular velocity increases from 5 rad/s to 15 rad/s.

[Ans: 100 rad] ✓

$$\alpha = 1 \text{ rad/s}^2$$

$$\Delta\theta = ?$$

$$\omega_0 = 5 \text{ rad/s}$$

$$\omega = 15 \text{ rad/s}$$

$$\omega^2 = \omega_0^2 + 2\alpha \cdot \Delta\theta$$

$$15^2 = 5^2 + 2 \times 1 \times \Delta\theta$$

$$225 = 25 + 2 \cdot \Delta\theta$$

$$200 = 2 \cdot \Delta\theta \Rightarrow \Delta\theta = \frac{200}{2} = 100 \text{ rad}$$

Ex3

A disc rotates about its axis with a constant angular acceleration of 4 rad/s². Find the radial and tangential accelerations of a particle at a distance of 1 cm from the axis at the end of the first second after the disc starts rotating.

[Ans: 16 cm/s², 4 cm/s²]

$$a_r = a_c = \omega^2 R$$

$$a_T = \alpha R$$

$$\alpha = 4 \text{ rad/s}^2$$

$$R = 1 \text{ cm.}$$



$$\text{Tangential acceleration } a_T = \alpha \cdot R = 4 \times 1 \text{ cm/s}^2$$

$$a_T = 4 \text{ cm/s}^2$$

$$\text{given at } t=0, \omega_0=0 ; t=1 \text{ sec, } \omega=?$$

$$t = 1 - 0 = 1 \text{ sec}$$

$$\omega = \omega_0 + \alpha t \Rightarrow \omega = 0 + 4 \times 1$$

$$\omega = 4 \text{ rad/s}$$

$$a_r = \omega^2 R = (4)^2 \cdot 1 \text{ cm/s}^2$$