

$$= \frac{m_1 \times 3R + 8m_1 \times 0}{m_1 + 8m_1} = \frac{3m_1 R}{9m_1} \Rightarrow \boxed{x_{cm} = \frac{R}{3}}$$

$$y_{cm} = 0 \quad (\because y_1 = y_2 = 0) \quad \boxed{CM = \left(\frac{R}{3}, 0\right)}$$

Motion of CM:

n-particle system

$$\begin{cases} \vec{v} = \frac{d\vec{r}}{dt} \\ \vec{a} = \frac{d\vec{v}}{dt} \end{cases}$$

$$m_1, m_2, m_3, \dots, m_n$$

$$\vec{r}_1, \vec{r}_2, \vec{r}_3, \dots, \vec{r}_n$$

$$\vec{r}_{cm} = \frac{1}{M} \cdot (m_1 \vec{r}_1 + m_2 \vec{r}_2 + \dots + m_n \vec{r}_n) \quad \text{--- (1)}$$

Differentiating Eq. (1) w.r.t time

$$\frac{d\vec{r}_{cm}}{dt} = \frac{1}{M} \frac{d}{dt} (m_1 \vec{r}_1 + m_2 \vec{r}_2 + \dots + m_n \vec{r}_n)$$

$$\vec{v}_{cm} = \frac{1}{M} \left\{ \frac{d}{dt} (m_1 \vec{r}_1) + \frac{d}{dt} (m_2 \vec{r}_2) + \dots + \frac{d}{dt} (m_n \vec{r}_n) \right\}$$

$$\vec{v}_{cm} = \frac{1}{M} \left\{ m_1 \frac{d\vec{r}_1}{dt} + m_2 \frac{d\vec{r}_2}{dt} + \dots + m_n \frac{d\vec{r}_n}{dt} \right\}$$

$$\checkmark \vec{v}_{cm} = \frac{1}{M} \{ m_1 \vec{v}_1 + m_2 \vec{v}_2 + \dots + m_n \vec{v}_n \} \quad \text{--- (2)}$$

Differentiating Eq. (2) w.r.t time

$$\frac{d\vec{v}_{cm}}{dt} = \frac{1}{M} \cdot \frac{d}{dt} (m_1 \vec{v}_1 + m_2 \vec{v}_2 + \dots + m_n \vec{v}_n)$$

$$= \frac{1}{M} \left\{ m_1 \frac{d\vec{v}_1}{dt} + m_2 \frac{d\vec{v}_2}{dt} + \dots + m_n \frac{d\vec{v}_n}{dt} \right\}$$

$$\checkmark \vec{a}_{cm} = \frac{1}{M} \{ m_1 \vec{a}_1 + m_2 \vec{a}_2 + \dots + m_n \vec{a}_n \} \quad \text{--- (3)}$$

$$M \vec{a}_{cm} = m_1 \vec{a}_1 + m_2 \vec{a}_2 + \dots + m_n \vec{a}_n \quad \text{--- (4)}$$

$$m_1 \vec{a}_1 = \vec{F}_1 + \vec{F}_1^{int}, \quad m_2 \vec{a}_2 = \vec{F}_2 + \vec{F}_2^{int}, \quad \dots \quad m_n \vec{a}_n = \vec{F}_n + \vec{F}_n^{int}$$

by Eq. (4)

$$M \vec{a}_{cm} = (\vec{F}_1 + \vec{F}_1^{int}) + (\vec{F}_2 + \vec{F}_2^{int}) + \dots + (\vec{F}_n + \vec{F}_n^{int})$$

$$M \vec{a}_{cm} = (\vec{F}_1 + \vec{F}_2 + \dots + \vec{F}_n) + (\vec{F}_1^{int} + \vec{F}_2^{int} + \dots + \vec{F}_n^{int})$$

$$M \vec{a}_{cm} = \vec{F}^{ext} + \sum \vec{F}^{int}$$

$$\therefore \text{For a system } \sum \vec{F}^{int} = 0 \Rightarrow \boxed{M \vec{a}_{cm} = \vec{F}^{ext}} \quad \text{--- (5)}$$

$$\checkmark m \vec{a} = \vec{F}$$