

According to this law, “the rate of change of momentum (mass × velocity) of a body is proportional to the impressed force and it takes place in the direction of the force”.

Mathematically  $\vec{F} \propto \frac{d\vec{p}}{dt} \Rightarrow \vec{F} = k \frac{d\vec{p}}{dt} = \frac{d\vec{p}}{dt}$

$$\vec{F} = \frac{d\vec{p}}{dt} \text{ (Defining force such a way that } k=1\text{)}$$

$$\vec{F} = \frac{d}{dt} (m\vec{v}) = m \frac{d\vec{v}}{dt} \text{ (consider mass } m \text{ is constant)}$$

$$\vec{F} = m \vec{a}$$

In scalar form,  $F = ma$

This equation is valid only if mass of the body is constant.

(i) Force is a vector quantity, whose unit is Newton or  $\frac{Kg.m}{sec^2}$  (In MKS)

and Dyne or  $\frac{gm \times cm}{sec^2}$  (In C. G. S.)

(ii) The dimension of force is  $(MLT^{-2})$

(iii) The second law of motion gives the magnitude and unit of force.

(iv) If  $m$  is not constant, then

$$\vec{F} = \frac{d}{dt} (m\vec{v}) = m \cdot \frac{d\vec{v}}{dt} + \vec{v} \frac{dm}{dt}$$

As in case of rocket propulsion, the mass of the fuel varies with respect to time.